

Parallel and Distributed Algorithms and Programs

TP n°2 - Sorting networks

Hadrien Croubois
hadrien.croubois@ens-lyon.fr

Aurélien Cavelan
aurelien.cavelan@ens-lyon.fr

25/09/2015

All documents are available on my website : <http://hadriencroubois.com/#Teaching>

Part 1

Distributed merge-sort

Consider we have an array A of size n and $p = 2^k$ nodes available to sort it. A is distributed among the different nodes so each one has $m = n/p$ elements. We call A_i the subset of A owned by each node i . At this stage you have no limitations on the amount of memory used or on the communications.

Question

- Initiate a random array that would be different on each node.
- Implement a C function that locally sorts an array of double :

```
void local_sort(double *A_i, size_t m);
```

- Think of an implementation of the merge sort algorithm that could work in our context. What is its complexity?
- Implement this algorithm using MPI. All program should call the `sort` function providing the same size.

```
void sort(double *A_i, size_t m, MPI_Comm comm);
```

Part 2

With some constraints

Here we add some constraint.

First of all, we are afraid our machines won't have a lot of memory space. Given the potentially large size of A we are not able to store all of it on a single machine. Therefore, our algorithm should not use more than twice the size needed to store A_i .

Also, we are working on a ring topology, so a node is only allowed to communicate with its neighbours $i - 1 \pmod n$ and $i + 1 \pmod n$.

Question

- Think of a new sorting algorithm that could work with our new restrictions. What is its complexity?
- Implement this algorithm using MPI. Try to optimize it as much as you can.

```
void sort_ring(double *A_i, size_t m, MPI_Comm comm);
```

Part 3

Evaluating performances

Question

- Think of a protocol for evaluating the performances of both algorithms. What are the parameters you would like to investigate?
- Run this protocol and compare the performances of your algorithms with other students.